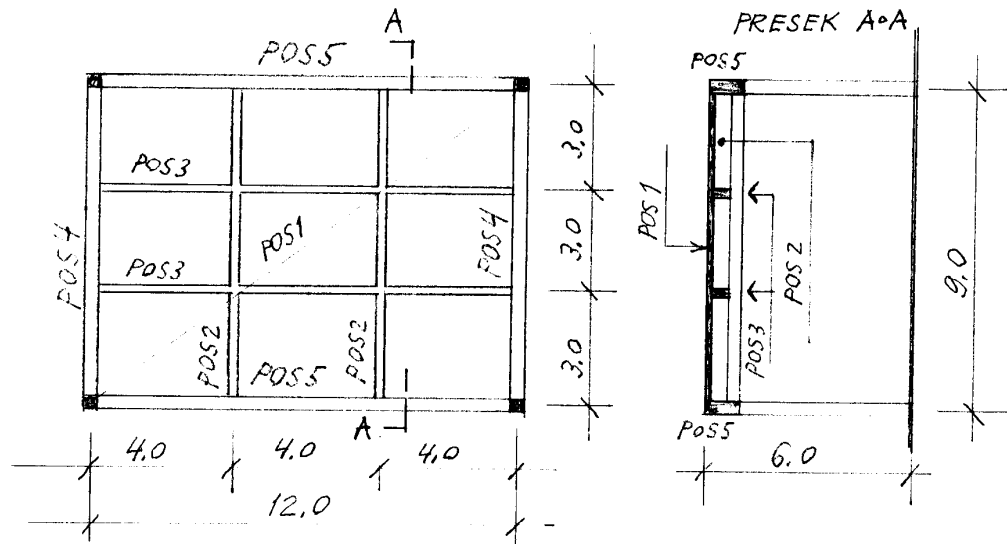


GRAĐEVINSKI FAKULTET
UNIVERZITET U BEOGRADU

Pismeni ispit 29.03.2008.

PROJEKTOVANJE I GRAĐENJE BETONSKIH KONSTRUKCIJA I



Za konstrukciju prikazanu na skici, za dejstvo totalnog opterećenja, potrebno je uraditi sledeće:

1. Dimenzionisati ploču POS 1 (dpl = 14cm) u karakterističnim presecima.
2. Izvršiti analizu opterećenja, sračunati i nacrtati dijagrame statičkih uticaja za grede POS 2 i POS 3 (b/d=30/50 cm). Dozvoljeno je osrednjiti opterećenje na gredama.
3. Odrediti potrebnu armaturu greda POS 2 i POS 3. Nacrtati raspored armature u poprečnom preseku.
4. Izvršiti analizu opterećenja, sračunati i nacrtati dijagrame statičkih uticaja za grede POS 4 i POS 5 (b/d=40/100 cm).
5. Odrediti potrebnu armaturu greda POS 4 i POS 5.

Podaci za proračun:

MB 30, RA 400/500
p=5.0 kN/m²

POS 1 – ploča $d_p = 14\text{ cm}$

$$g = 0.14 \times 25 = 3.5\text{ kN/m}^2 \quad ; \quad p = 5\text{ kN/m}^2$$

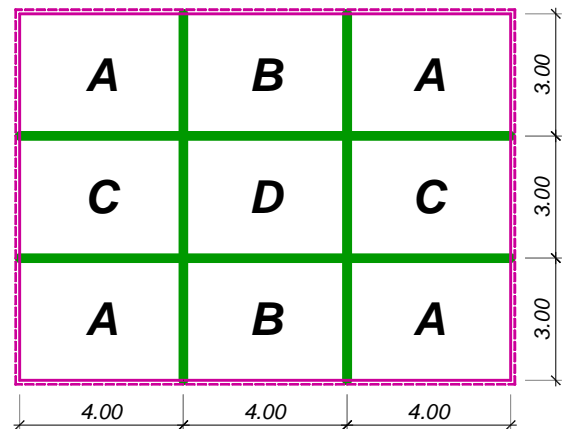
za sve delove ploče:

$$L_y/L_x = 4.0/3.0 = 1.33 \approx 1.3$$

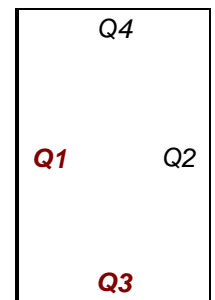
$$G = 3.5 \times 4.0 \times 3.0 = 42\text{ kN}$$

$$P = 5.0 \times 4.0 \times 3.0 = 60\text{ kN}$$

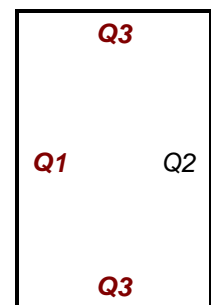
$$Q_u = 1.6 \times 42 + 1.8 \times 60 = 175.6\text{ kN}$$

**ploča tipa »A«**

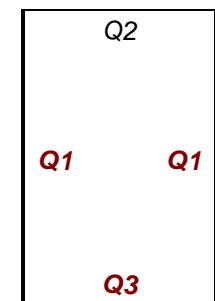
$L_y/L_x = 1.3$			G	P	U	L	g_i	p_i
k			kN	kN	kN	m	kN/m	kN/m
duža strana, uklještenje	0.346	Q_1	14.5	20.8		4.00	3.63	5.19
duža strana, oslonac	0.233	Q_2	9.8	14.0		4.00	2.45	3.50
kraća strana, uklještenje	0.244	Q_3	10.2	14.6		3.00	3.42	4.88
kraća strana, oslonac	0.177	Q_4	7.4	10.6		3.00	2.48	3.54
kraći pravac, polje	0.032	M_x	1.34	1.92	5.61			kNm/m
duži pravac, polje	0.021	M_y	0.88	1.26	3.68			kNm/m
kraći pravac, oslonac	0.071	X	2.98	4.26	12.44			kNm/m
duži pravac, oslonac	0.059	Y	2.48	3.54	10.34			kNm/m

**ploča tipa »B«**

$L_y/L_x = 1.3$			G	P	U	L	g_i	p_i
k			kN	kN	kN	m	kN/m	kN/m
duža strana, uklještenje	0.316	Q_1	13.3	19.0		4.00	3.32	4.74
duža strana, oslonac	0.218	Q_2	9.2	13.1		4.00	2.29	3.27
kraća strana, uklještenje	0.233	Q_3	9.8	14.0		3.00	3.26	4.66
kraći pravac, polje	0.028	M_x	1.18	1.68	4.91			kNm/m
duži pravac, polje	0.022	M_y	0.92	1.32	3.85			kNm/m
kraći pravac, oslonac	0.063	X	2.65	3.78	11.04			kNm/m
duži pravac, oslonac	0.055	Y	2.31	3.30	9.64			kNm/m

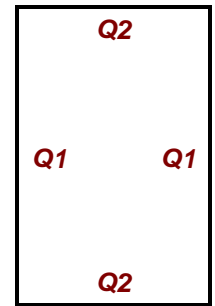
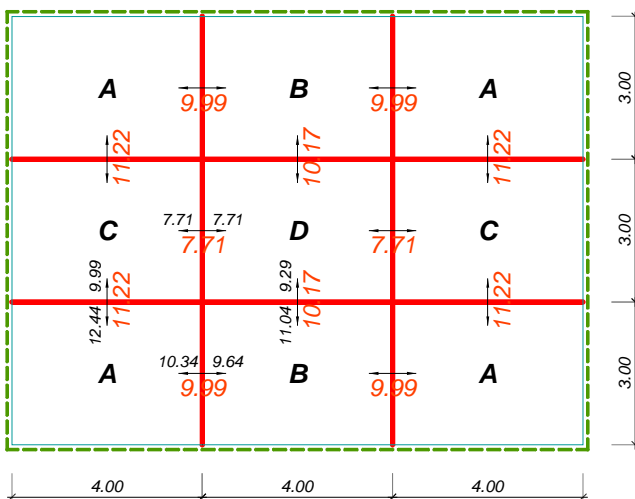
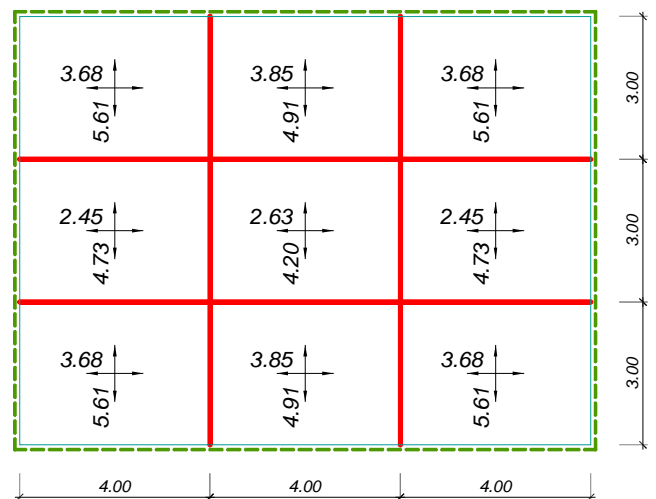
**ploča tipa »C«**

$L_y/L_x = 1.3$			G	P	U	L	g_i	p_i
k			kN	kN	kN	m	kN/m	kN/m
duža strana, uklještenje	0.309	Q_1	13.0	18.5		4.00	3.24	4.64
kraća strana, oslonac	0.165	Q_2	6.9	9.9		3.00	2.31	3.30
kraća strana, uklještenje	0.217	Q_3	9.1	13.0		3.00	3.04	4.34
kraći pravac, polje	0.027	M_x	1.13	1.62	4.73			kNm/m
duži pravac, polje	0.014	M_y	0.59	0.84	2.45			kNm/m
kraći pravac, oslonac	0.057	X	2.39	3.42	9.99			kNm/m
duži pravac, oslonac	0.044	Y	1.85	2.64	7.71			kNm/m



ploča tipa »D«

$L_y/L_x = 1.3$			G	P	U	L	g_i	p_i
		k	kN	kN	kN	m	kN/m	kN/m
duža strana, uklještenje	0.291	Q_1	12.2	17.5		4.00	3.06	4.37
kraća strana, uklještenje	0.209	Q_2	8.8	12.5		3.00	2.93	4.18
kraći pravac, polje	0.024	M_x	1.01	1.44	4.20	kNm/m		
duži pravac, polje	0.015	M_y	0.63	0.90	2.63	kNm/m		
kraći pravac, oslonac	0.053	X	2.23	3.18	9.29	kNm/m		
duži pravac, oslonac	0.044	Y	1.85	2.64	7.71	kNm/m		

 M_u [kNm/m] - GORNJA ZONA M_u [kNm/m] - DONJA ZONADimenzionisanje

MB 30 $\bar{f}_B = 20.5 \text{ MPa}$; RA 400/500 $\bar{f}_{sv} = 400 \text{ MPa}$

$\max. M_u = M_{yu} = 11.22 \text{ kNm/m}$ (upravno na POS 3 - oslonac između ploča A i C)

$a_{1y} = 2.5 \text{ cm}$ $\bar{d} \quad h_y = d - a_{1y} = 14 - 2.5 = 11.5 \text{ cm}$

$$k = \frac{11.5}{\sqrt{\frac{11.22 \times 10^2}{100 \times 2.05}}} = 4.916 \quad \Rightarrow \quad e_b/e_a = 1.075/10\text{‰} ; \quad \bar{\mu} = 4.285\%$$

$$A_{ay} = 4.285 \times \frac{100 \times 11.5}{100} \times \frac{2.05}{40} = 2.53 \text{ cm}^2/\text{m} > A_{a,\min.} = 0.1 \times 14 = 1.4 \text{ cm}^2/\text{m}$$

$$\text{pretp. } \emptyset 8 (a_a^{(1)} = 0.503 \text{ cm}^2/\text{m}) \quad \Rightarrow \quad e_a = \frac{100 \times a_a^{(1)}}{A_a} = \frac{100 \times 0.503}{2.53} = 19.9 \text{ cm}$$

usvojeno: **RØ8/15** (3.35 cm²/m)

$$A_{ap} = 0.2 \times 2.53 = 0.51 \text{ cm}^2/\text{m} < A_{ap,\min.} = 0.085 \times 14 = 1.19 \text{ cm}^2/\text{m}$$

$$\text{pretp. } \emptyset 8 (a_{ap}^{(1)} = 0.503 \text{ cm}^2/\text{m}) \quad \Rightarrow \quad e_{ap} = \frac{100 \times a_{ap}^{(1)}}{A_{ap}} = \frac{100 \times 0.503}{1.19} = 42.2 \text{ cm}$$

usvojeno: **RØ8/30** (1.68 cm²/m)

$\max.M_{xu} = 9.99 \text{ kNm/m}$ (upravno na POS 2 - oslonac između ploča A i B)

$h_x = h_y - (\varnothing_x + \varnothing_y)/2 = 11.5 - 0.8 = 10.7 \text{ cm}$

$$k = \frac{10.7}{\sqrt{\frac{9.99 \times 10^2}{100 \times 2.05}}} = 4.847 \Rightarrow e_b/e_a = 1.094/10\text{‰} ; \bar{\mu} = 4.409\%$$

$$A_{ax} = 4.847 \times \frac{100 \times 10.7}{100} \times \frac{2.05}{40} = 2.44 \text{ cm}^2/\text{m} > A_{a,\min.} = 0.1 \times 14 = 1.4 \text{ cm}^2/\text{m}$$

usvojeno: **RØ8/15** ($3.35 \text{ cm}^2/\text{m}$)

usvojeno: **RØ8/30** ($1.68 \text{ cm}^2/\text{m}$) – podeona armatura

S obzirom na veoma male vrednosti graničnih računskih momenata savijanja u donjoj zoni, biće usvojena minimalna armatura. Minimalni raspoloživi profil armature je RØ8 a maksimalno dopušteno rastojanje šipki 20 cm, pa sledi:

$$RØ8/20 \Rightarrow A_a = \frac{100 \times a_a^{(1)}}{e_a} = \frac{100 \times 0.503}{20} = 2.51 \frac{\text{cm}^2}{\text{m}} > A_{a,\min.} = 0.1 \times 14 = 1.4 \text{ cm}^2/\text{m}$$

Nosivost ovako usvojene armature, sračunato sa približnom vrednošću kraka unutrašnjih sila koji odgovara manjoj statičkoj visini $z \approx 0.9 \times 10.7 = 9.63 \text{ cm}$, je:

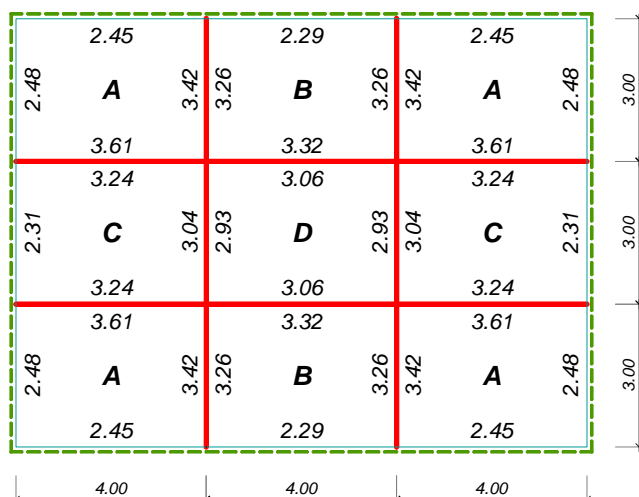
$$M_u \approx 2.51 \times 9.63 \times 10^{-2} \times 40 = 9.68 \text{ kNm/m} > M_{u,\max} = 5.61 \text{ kNm/m}$$

usvojeno: **RØ8/20** ($2.51 \text{ cm}^2/\text{m}$) - donja zona, oba pravca

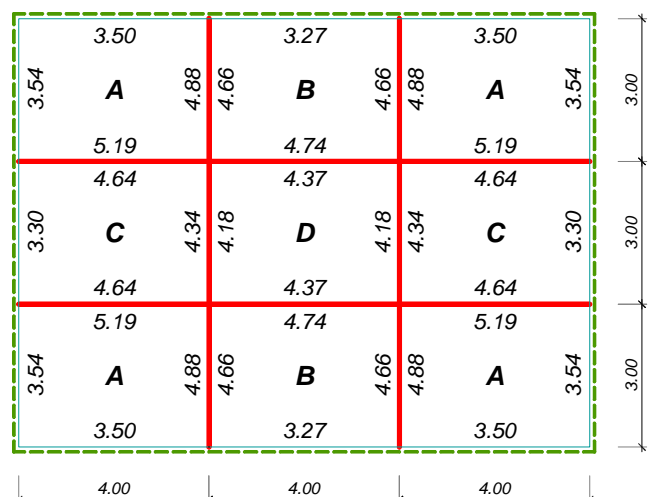
POS 2, POS 3 – grede b/d = 30/50 cm

Opterećenje sa POS 1 na pojedine grede:

STALNO OPTEREĆENJE [kN/m]



POVREMENO OPTEREĆENJE [kN/m]



Sopstvenu težinu gređa POS 2 i POS 3, odnosno POS 4 i POS 5:

$$g_{2,3} = 0.3 \times 0.5 \times 25 = 3.75 \text{ kN/m} \quad g_{4,5} = 0.4 \times 1.0 \times 25 = 10.0 \text{ kN/m}$$

treba dodati prikazanom stalnom opterećenju sa POS 1.

Ovako sračunata opterećenja po pojedinim poljima će, prema uslovu zadatka, biti osrednjena posebno za svaku pojedinačnu gređu.

grede POS 2:

$$g_1 = 3.42 + 3.26 + 3.75 = 10.43 \text{ kN/m} = g_3 ; \quad p_1 = 4.88 + 4.66 = 9.54 \text{ kN/m} = p_3$$

$$g_2 = 3.04 + 2.93 + 3.75 = 9.72 \text{ kN/m} \quad ; \quad p_2 = 4.34 + 4.18 = 8.52 \text{ kN/m}$$

$$g^{\text{POS2}} = \frac{2 \times 10.43 + 9.72}{3} = 10.19 \text{ kN/m} \quad ; \quad p^{\text{POS2}} = \frac{2 \times 9.54 + 8.52}{3} = 9.2 \text{ kN/m}$$

grede POS 3:

$$g_1 = 3.24 + 3.61 + 3.75 = 10.6 \text{ kN/m} = g_3 ; \quad p_1 = 5.19 + 4.64 = 9.83 \text{ kN/m} = p_3$$

$$g_2 = 3.06 + 3.32 + 3.75 = 10.13 \text{ kN/m} \quad ; \quad p_2 = 4.74 + 4.37 = 9.11 \text{ kN/m}$$

$$g^{\text{POS3}} = \frac{2 \times 10.6 + 10.13}{3} = 10.44 \text{ kN/m} \quad ; \quad p^{\text{POS3}} = \frac{2 \times 9.83 + 9.11}{3} = 9.59 \text{ kN/m}$$

grede POS 4:

$$g_1 = 2.48 + 10.0 = 12.48 \text{ kN/m} = g_3 \quad ; \quad p_1 = 3.54 \text{ kN/m} = p_3$$

$$g_2 = 2.31 + 10.0 = 12.31 \text{ kN/m} \quad ; \quad p_2 = 3.30 \text{ kN/m}$$

$$g^{\text{POS4}} = \frac{2 \times 12.48 + 12.31}{3} = 12.42 \text{ kN/m} \quad ; \quad p^{\text{POS4}} = \frac{2 \times 3.54 + 3.30}{3} = 3.46 \text{ kN/m}$$

grede POS 5:

$$g_1 = 2.45 + 10.0 = 12.45 \text{ kN/m} = g_3 \quad ; \quad p_1 = 3.50 \text{ kN/m} = p_3$$

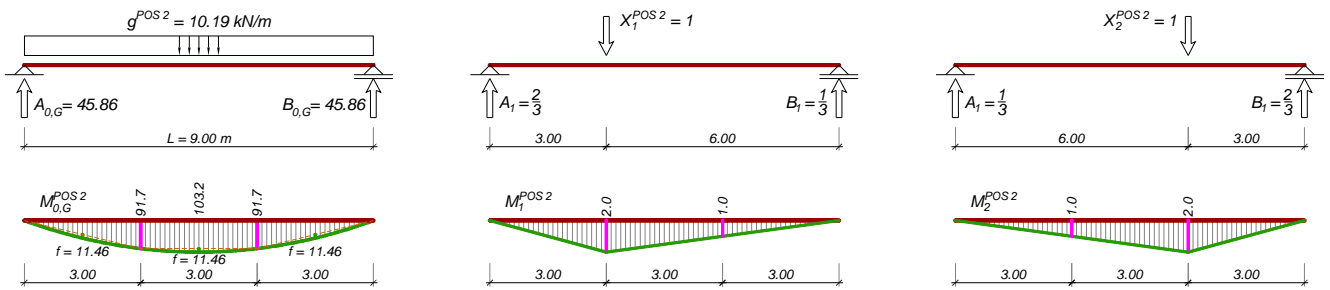
$$g_2 = 2.29 + 10.0 = 12.29 \text{ kN/m} \quad ; \quad p_2 = 3.27 \text{ kN/m}$$

$$g^{\text{POS5}} = \frac{2 \times 12.45 + 12.29}{3} = 12.40 \text{ kN/m} \quad ; \quad p^{\text{POS5}} = \frac{2 \times 3.50 + 3.27}{3} = 3.42 \text{ kN/m}$$

Kod izbora statičkog sistema za proračun greda POS 2 do POS 5, treba zapaziti sledeće:

- konstrukcija se oslanja samo na 4 ugaona stuba, pa se mora sračunati kao roštiljna;
- grede POS 2 i POS 3 ($b/d=30/50 \text{ cm}$) su daleko manje krutosti od greda POS 4 i POS 5 ($b/d=40/100 \text{ cm}$). Stoga se može smatrati da su grede POS 4 i POS 5 vertikalni oslonci za POS 2 i POS 3;
- Torziona krutost greda POS 4 i POS 5 određena je prvenstveno manjom dimenzijom preseka i nije realno da, naročito u stanju sa prslinama, ove grede predstavljaju uklještenja (potpuno spreče rotaciju) krajeva greda POS 2 i POS 3. Slično, ove grede ne mogu jedna drugoj predstavljati uklještenje niti biti uklještenene u stubove datih dimenzija (sa crteža očito $40/40 \text{ cm}$) pa sledi da su POS 4 i POS 5 proste grede raspona 9.0 odnosno 12.0 m, opterećene opterećenjem sa ploče POS 1 i u trećinama raspona reakcijama greda POS 3, odnosno POS 2.
- grede POS 2 i POS 3 su iste krutosti, opterećene približno jednakim opterećenjem ali različitih raspona, pa se moraju proračunati kao roštiljna konstrukcija. Kao statički nepoznate se usvajaju vertikalne sile u presečnim tačkama, a sračunavaju se metodom sila, izjednačavanjem deformacija presečnih tačaka. Zbog simetrije je jasno da su sve nepoznate sile X_i jednake.

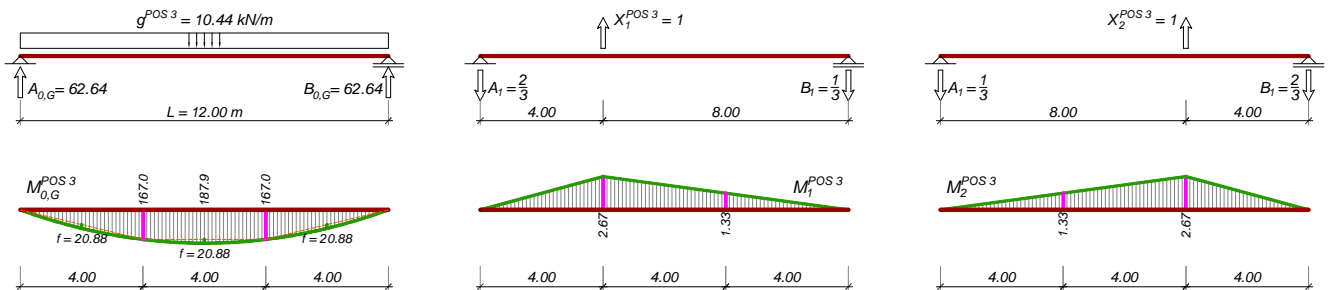
U nastavku je prikazan proračun statičkih uticaja za grede POS 2 i POS 3 i prikazani dijagrami momenata savijanja i transverzalnih sila usled stalnog (G), povremenog (P) i graničnog računskog (U) opterećenja.



$$EI\delta_{11}^{\text{POS2}} = \frac{9.0}{3} \times 2.0^2 = 12.0 = EI\delta_{22}^{\text{POS2}}$$

$$EI\delta_{12}^{\text{POS2}} = 2 \times \frac{3.0}{3} \times 2.0 \times 1.0 + \frac{3.0}{6} \times [2.0 \times (2 \times 1.0 + 2.0) + 1.0 \times (2 \times 2.0 + 1.0)] = 10.5 = EI\delta_{21}^{\text{POS2}}$$

$$EI\delta_{10,G}^{\text{POS2}} = \frac{3.0}{3} \times (91.7 \times 2.0 + 91.7 \times 1.0) + \frac{3.0}{3} \times 11.46 \times (1.0 + 2.0) + \frac{3.0}{2} \times 91.7 \times (2.0 + 1.0) + \frac{3.0}{3} \times 11.46 \times (2.0 + 1.0) = 275.1 + 34.4 + 412.7 + 34.4 = 756.6 = EI\delta_{20,G}^{\text{POS2}}$$



$$EI\delta_{11}^{\text{POS3}} = \frac{12.0}{3} \times 2.67^2 = 28.44 = EI\delta_{22}^{\text{POS3}}$$

$$EI\delta_{12}^{\text{POS3}} = 2 \times \frac{4.0}{3} \times 2.67 \times 1.33 + \frac{4.0}{6} \times [2.67 \times (2 \times 1.33 + 2.67) + 1.33 \times (2 \times 2.67 + 1.33)] = 24.89$$

$$-EI\delta_{10,G}^{\text{POS3}} = \frac{4.0}{3} \times (167.0 \times 2.67 + 167.0 \times 1.33) + \frac{4.0}{3} \times 20.88 \times (1.33 + 2.67) + \frac{4.0}{2} \times 167.0 \times (2.67 + 1.33) + \frac{4.0}{3} \times 20.88 \times (2.67 + 1.33) = 890.9 + 111.4 + 1336.3 + 111.4 = 2449.9 = -EI\delta_{20,G}^{\text{POS3}}$$

$$EI\delta_{11} = EI\delta_{11}^{\text{POS2}} + EI\delta_{11}^{\text{POS3}} = 12.0 + 28.44 = 40.44 = EI\delta_{22}$$

$$EI\delta_{12} = EI\delta_{12}^{\text{POS2}} + EI\delta_{12}^{\text{POS3}} = 10.5 + 24.89 = 35.39 = EI\delta_{21}$$

$$EI\delta_{10,G} = EI\delta_{10,G}^{\text{POS2}} + EI\delta_{10,G}^{\text{POS3}} = 756.6 - 2449.9 = -1693.3 = EI\delta_{20,G}$$

$$\left. \begin{aligned} EI\delta_{11} \cdot X_{1G} + EI\delta_{12} \cdot X_{2G} + EI\delta_{10,G} &= 0 \\ EI\delta_{21} \cdot X_{1G} + EI\delta_{22} \cdot X_{2G} + EI\delta_{20,G} &= 0 \end{aligned} \right\} \Rightarrow X_{1G} = -\frac{-1693.3}{40.44 + 35.39} = 22.33 \text{ kN} = X_{2G}$$

Sile koje se prenose na POS 5 (sa POS 2), odnosno POS 4 (sa POS 3):

$$G^{\text{POS2}} = 45.86 + \frac{2}{3} \times 22.33 + \frac{1}{3} \times 22.33 = 68.18 \text{ kN}$$

$$G^{\text{POS3}} = 62.64 + \left(-\frac{2}{3}\right) \times 22.33 + \left(-\frac{1}{3}\right) \times 22.33 = 40.31 \text{ kN}$$

Analogno se proračunavaju uticaji usled povremenog opterećenja:

$$EI\delta_{10,P}^{POS2} = \frac{p_2}{g_2} \times EI\delta_{10,G}^{POS2} = \frac{9.20}{10.19} \times 756.6 = 683.1$$

$$EI\delta_{10,P}^{POS3} = \frac{p_3}{g_3} \times EI\delta_{10,G}^{POS3} = \frac{9.59}{10.44} \times (-2449.9) = -2250.5$$

$$EI\delta_{10,P} = EI\delta_{10,P}^{POS2} + EI\delta_{10,P}^{POS3} = 683.1 - 2250.5 = -1567.4 = EI\delta_{20,P}$$

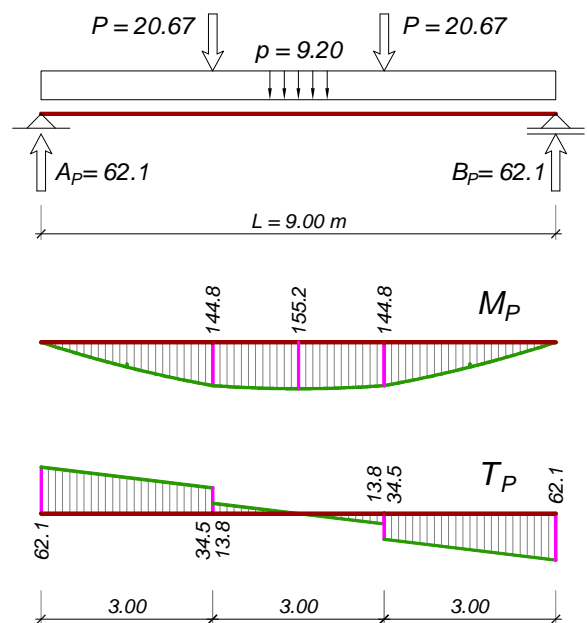
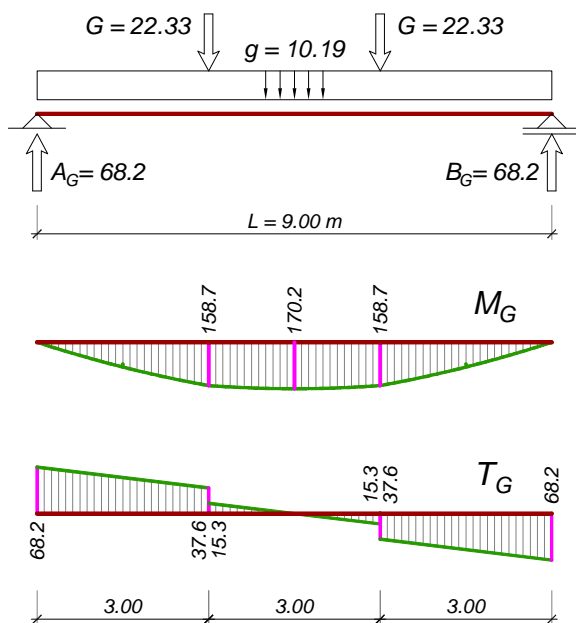
$$X_{1P} = -\frac{-1567.4}{40.44 + 35.39} = 20.67 \text{ kN} = X_{2P}$$

Sile koje se prenose na POS 5 (sa POS 2), odnosno POS 4 (sa POS 3):

$$P^{POS2} = 9.20 \times \frac{9.0}{2} + \frac{2}{3} \times 20.67 + \frac{1}{3} \times 20.67 = 62.07 \text{ kN}$$

$$P^{POS3} = 9.59 \times \frac{12.0}{2} + \left(-\frac{2}{3}\right) \times 20.67 + \left(-\frac{1}{3}\right) \times 20.67 = 36.87 \text{ kN}$$

Dimenzionisanje POS 2



$$M_u = 1.6 \times 170.2 + 1.8 \times 155.2 = 551.5 \text{ kNm}$$

$$B = \min \left\{ \begin{array}{l} 30 + 0.25 \times 900 = 255 \\ 30 + 20 \times 14 = 310 \end{array} \right\} = 255 \text{ cm}$$

$$\text{pretp. } a_1 = 7 \text{ cm} \Rightarrow h = 50 - 7 = 43 \text{ cm}$$

$$k = \frac{43}{\sqrt{\frac{551.5 \times 10^2}{255 \times 2.05}}} = 3.211 \Rightarrow \varepsilon_b / \varepsilon_b = 1.892 / 10\% \Rightarrow s = 0.159 \Rightarrow x = 0.159 \times 43 = 6.8 \text{ cm} < 14 \text{ cm}$$

$$\bar{\mu} = 10.308\%$$

$$A_a = 10.308 \times \frac{255 \times 43}{100} \times \frac{2.05}{40} = 34.07 \text{ cm}^2 \Rightarrow \text{usvojeno } 8R\emptyset 25 \text{ (39.27 cm}^2\text{)}$$

$$T_u^A = 1.6 \times 68.2 + 1.8 \times 62.1 = 220.8 \text{ kN}$$

$$\tau_n^A = \frac{220.8}{30 \times 0.9 \times 43} = 0.190 \frac{\text{kN}}{\text{cm}^2} = 1.90 \text{ MPa} \quad \left\{ \begin{array}{l} > \tau_r = 1.1 \text{ MPa} \\ < 3\tau_r \end{array} \right.$$

$$T_u^B = 1.6 \times 37.6 + 1.8 \times 34.5 = 122.2 \text{ kN}$$

$$\tau_n^B = \frac{122.2}{30 \times 0.9 \times 43} = 0.105 \frac{\text{kN}}{\text{cm}^2} = 1.05 \text{ MPa} < \tau_r$$

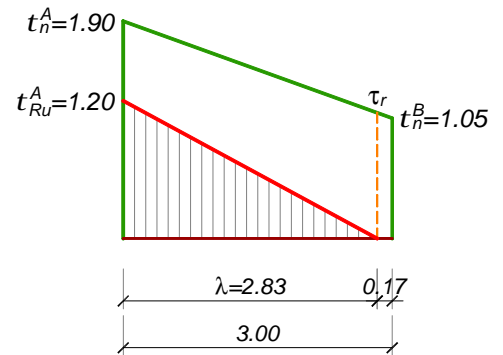
$$\lambda = \frac{1.90 - 1.1}{1.90 - 1.05} \times 3.0 = 2.83 \text{ m}$$

$$\tau_{Ru}^A = \frac{3}{2} \times (0.190 - 0.11) = 0.12 \frac{\text{kN}}{\text{cm}^2} \Rightarrow e_u = \frac{2 \times 0.503}{30 \times 0.120} \times 40 = 11.1 \text{ cm}$$

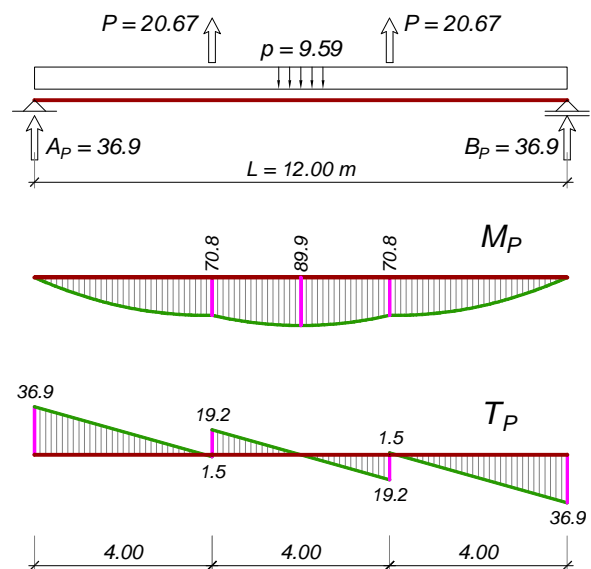
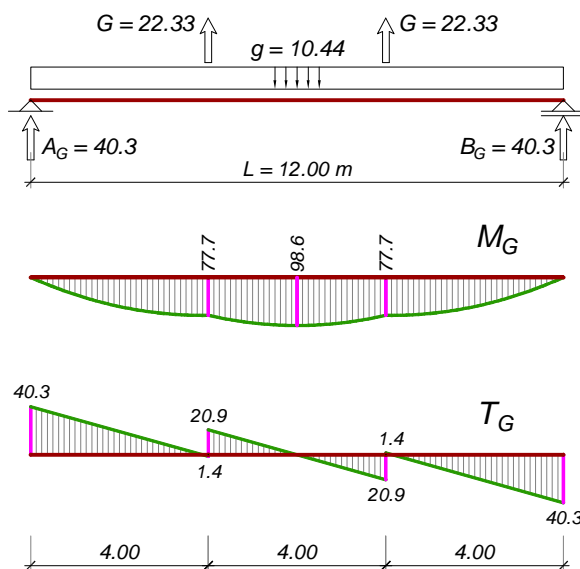
usvojeno **URØ8/10** ($m=2$)

$$\Delta A_a = \frac{220.8}{2 \times 40} \times (\text{ctg} 45^\circ - \text{ctg} 90^\circ) = 2.76 \text{ cm}^2$$

Preko slobodnog oslonca prevodi se minimalno trećina armature iz polja, tj. **4RØ25**.



Dimenzionisanje POS 3



$$M_u = 1.6 \times 98.6 + 1.8 \times 89.9 = 319.7 \text{ kNm}$$

$$B = \min \left\{ \begin{array}{l} 30 + 0.25 \times 1200 = 330 \\ 30 + 20 \times 14 = 310 \end{array} \right\} = 310 \text{ cm} \quad ; \quad \text{pretp. } a_1 = 7 \text{ cm} \Rightarrow h = 50 - 7 = 43 \text{ cm}$$

$$k = \frac{43}{\sqrt{\frac{319.7 \times 10^2}{310 \times 2.05}}} = 4.217 \Rightarrow s = 0.115 \Rightarrow x = 0.115 \times 43 = 4.95 \text{ cm} < 14 \text{ cm}$$

$$\bar{\mu} = 5.863\%$$

$$A_a = 5.863 \times \frac{310 \times 43}{100} \times \frac{2.05}{40} = 19.38 \text{ cm}^2 \Rightarrow \text{usvojeno } \mathbf{6RØ22} \text{ (22.81 cm}^2\text{)}$$

$$T_{u,max} = 1.6 \times 40.3 + 1.8 \times 36.9 = 130.9 \text{ kN}$$

$$\tau_n = \frac{130.9}{30 \times 0.9 \times 43} = 0.113 \frac{\text{kN}}{\text{cm}^2} = 1.13 \text{ MPa} \begin{cases} > \tau_r = 1.1 \text{ MPa} \\ < 3\tau_r \end{cases}$$

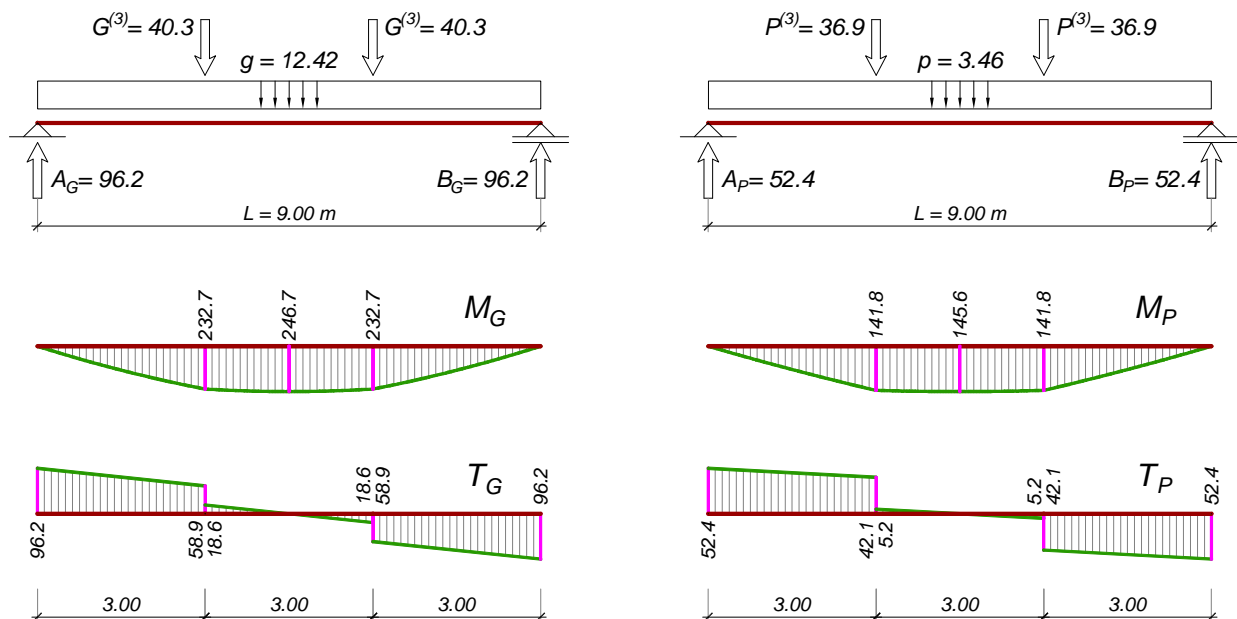
$$\tau_{Ru} = \frac{3}{2} \times (0.113 - 0.11) = 0.04 \frac{\text{kN}}{\text{cm}^2} \Rightarrow e_u = \frac{2 \times 0.503}{30 \times 0.2 \times 10^{-2}} = 16.7 \text{ cm}$$

usvojeno **URØ8/15** ($m=2$) na $\lambda \approx 1.0 \text{ m}$

$$\Delta A_a = \frac{130.9}{2 \times 40} \times (\text{ctg}45^\circ - \text{ctg}90^\circ) = 1.64 \text{ cm}^2$$

Preko slobodnog oslonca prevodi se minimalno trećina armature iz polja, tj. **2RØ22**.

Dimenzionisanje POS 4



$$M_u = 1.6 \times 246.7 + 1.8 \times 145.6 = 656.9 \text{ kNm}$$

$$B = \min \left\{ \begin{array}{l} 40 + 0.25 \times 900 / 3 = 115 \\ 40 + 8 \times 14 = 152 \end{array} \right\} = 115 \text{ cm} ; \text{ pretp. } a_1 = 7 \text{ cm} \Rightarrow h = 100 - 7 = 93 \text{ cm}$$

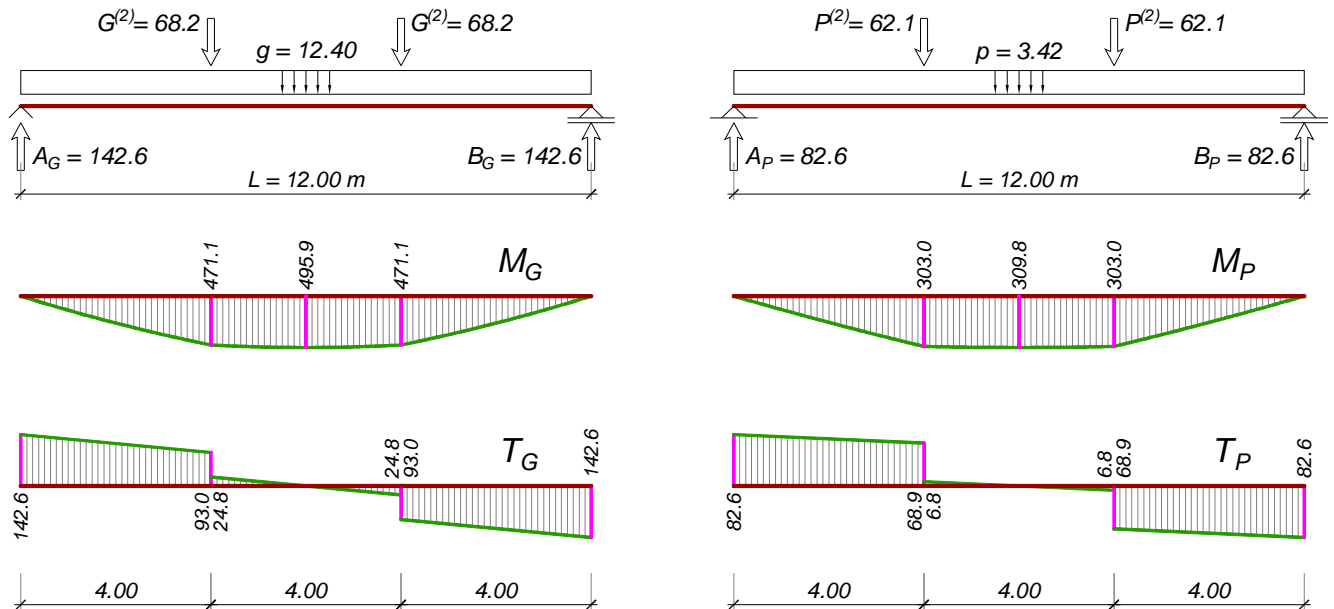
$$k = \frac{93}{\sqrt{\frac{656.9 \times 10^2}{115 \times 2.05}}} = 6.363 \Rightarrow s = 0.074 \Rightarrow x = 0.074 \times 93 = 6.84 \text{ cm} < 14 \text{ cm}$$

$$\bar{\mu} = 2.535\% \quad \varepsilon_b / \varepsilon_b = 0.794 / 10\%$$

$$A_a = 2.535 \times \frac{115 \times 93}{100} \times \frac{2.05}{40} = 18.12 \text{ cm}^2 \Rightarrow \text{usvojeno } \mathbf{5RØ22} \text{ (19.00 cm}^2\text{)}$$

$$T_{u,max} = 1.6 \times 96.2 + 1.8 \times 52.4 = 248.3 \text{ kN}$$

$$\tau_n = \frac{248.3}{40 \times 0.9 \times 93} = 0.074 \frac{\text{kN}}{\text{cm}^2} < \tau_r \quad \text{- nije potrebno osiguranje armaturom}$$

Dimenzionisanje POS 5

$$M_u = 1.6 \times 495.9 + 1.8 \times 309.8 = 1351.2 \text{ kNm}$$

$$B = \min \left\{ \begin{array}{l} 40 + 0.25 \times 1200 / 3 = 140 \\ 40 + 8 \times 14 = 152 \end{array} \right\} = 140 \text{ cm} ; \text{ pretp. } a_1 = 7 \text{ cm} \Rightarrow h = 100 - 7 = 93 \text{ cm}$$

$$k = \frac{93}{\sqrt{\frac{1351.2 \times 10^2}{140 \times 2.05}}} = 4.437 \Rightarrow s = 0.109 \Rightarrow x = 0.109 \times 93 = 10.1 \text{ cm} < 14 \text{ cm}$$

$$\bar{\mu} = 5.283\%$$

$$A_a = 5.283 \times \frac{140 \times 93}{100} \times \frac{2.05}{40} = 37.77 \text{ cm}^2 \Rightarrow \text{usvojeno } \mathbf{8R\text{\O}25} \text{ (39.27 cm}^2\text{)}$$

$$T_{u,max} = 1.6 \times 142.6 + 1.8 \times 82.6 = 376.8 \text{ kN}$$

$$\tau_n = \frac{376.8}{40 \times 0.9 \times 93} = 0.113 \frac{\text{kN}}{\text{cm}^2} = 1.13 \text{ MPa} \left\{ \begin{array}{l} > \tau_r = 1.1 \text{ MPa} \\ < 3\tau_r \end{array} \right.$$

$$\tau_{Ru} = \frac{3}{2} \times (0.113 - 0.11) = 0.04 \frac{\text{kN}}{\text{cm}^2} \Rightarrow e_u = \frac{2 \times 0.785}{40 \times 0.2 \times 10^{-2}} = 19.6 \text{ cm}$$

usvojeno **UR\text{\O}10/15** ($m=2$) na $\lambda \approx 1.0$ m

$$\Delta A_a = \frac{376.8}{2 \times 40} \times (\text{ctg}45^\circ - \text{ctg}90^\circ) = 4.71 \text{ cm}^2$$

Preko slobodnog oslonca prevodi se minimalno trećina armature iz polja, tj. **3R\text{\O}25**.