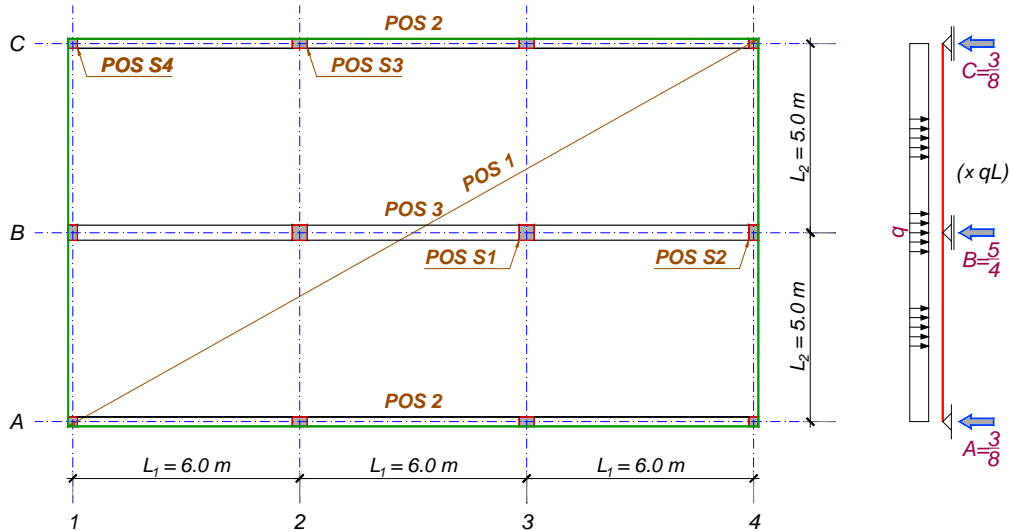


Ploča POS 1 na gredama u jednom pravcu

1



1.2 ANALIZA OPTEREĆENJA ZA POS 1

2

- sopstvena težina ploče	0.14×25	$= 3.5 \text{ kN/m}^2$
- dodatno stalno opterećenje	Δg	$= 2.5 \text{ kN/m}^2$
ukupno, stalno opterećenje	g	$= 6.0 \text{ kN/m}^2$
повремено opterećenje:	p	$= 4.0 \text{ kN/m}^2$

1.3 STATIČKI UTICAJI ZA POS 1

Reakcije oslonaca se računavaju za svako pojedinačno opterećenje:

- na gredu POS 2:

$$A_g = 0.375 \times 6.0 \times 5.0 = 11.25 \text{ kN/m}$$

$$A_p = 0.375 \times 4.0 \times 5.0 = 7.5 \text{ kN/m}$$

- na gredu POS 3:

$$B_g = 1.25 \times 6.0 \times 5.0 = 37.5 \text{ kN/m}$$

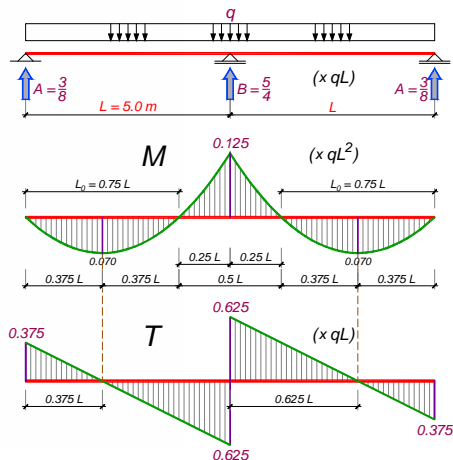
$$B_p = 1.25 \times 4.0 \times 5.0 = 25.0 \text{ kN/m}$$

dok je momente savijanja i transverzalne sile dovoljno računati samo za granično opterećenje ukoliko se ne vrši kontrola napona, prslina i ugiba (graničnih stanja upotrebljivosti):

$$q_u = 1.6 \times 6.0 + 1.8 \times 4.0 = 16.8 \text{ kN/m}^2$$

$$M_{u,1} = 16.8 \times 5.0^2 / 8 = 52.5 \text{ kNm/m}$$

$$M_{u,01} = 0.07 \times 16.8 \times 5.0^2 = 29.5 \text{ kNm/m}$$



2.2 ANALIZA OPTEREĆENJA ZA POS 3

Uobičajena visina greda je:

$$d \approx \frac{L}{10} \div \frac{L}{12} = \frac{600}{10} \div \frac{600}{12} = 60 \div 50 \text{ cm} \Rightarrow \text{pretp. } d = 50 \text{ cm}$$

Sa pretpostavljenom širinom grede POS 3 od $b = 40 \text{ cm}$, sledi:

- sopstvena težina POS 3 $0.4 \times 0.5 \times 25 = 5.0 \text{ kN/m}$
- stalno opterećenje od POS 1 $B_g = 37.5 \text{ kN/m}$
- ukupno, stalno opterećenje $g = 42.5 \text{ kN/m}$
- povremeno opterećenje od POS 1: $B_p = p = 25.0 \text{ kN/m}$

2.3 PRELIMINARNO DIMENZIONISANJE POS 3

$$q_u = 1.6 \times 42.5 + 1.8 \times 25.0 = 113 \text{ kN/m}$$

$$M_{u,1} = 113 \times 6.0^2 / 10 = 406.8 \text{ kNm} \quad \text{- gornja zona, oslonac}$$

$$k = \frac{43}{\sqrt{\frac{406.8 \times 10^2}{40 \times 2.05}}} = 1.931 \Rightarrow \begin{cases} \varepsilon_b / \varepsilon_a = 3.5 / 5.316\% \\ \mu = 32.138\% \end{cases}$$

$$A_a = 32.138 \times \frac{40 \times 43}{100} \times \frac{2.05}{40} = 28.33 \text{ cm}^2 \Rightarrow \text{usv.: } \mathbf{8R\check{O}22} \quad (30.41 \text{ cm}^2)$$

2.3.2 Kontrola glavnih napona zatezanja

$$T_u^{B,levo} = 0.6 \times 113 \times 6.0 = 406.8 \text{ kN} \Rightarrow \tau_n^{B,l} = \frac{406.8}{40 \times 0.9 \times 43} = 0.263 \frac{\text{kN}}{\text{cm}^2} \left\{ \begin{array}{l} > \tau_r \\ < 3\tau_r \end{array} \right.$$

$$\lambda = 0.6 \times 600 \times \left(1 - \frac{0.11}{0.263}\right) = 209.3 \text{ cm}; \quad \tau_{Ru}^{B,l} = \frac{3}{2} \times (0.263 - 0.11) = 0.229 \frac{\text{kN}}{\text{cm}^2}$$

$$m = 2; \alpha = 90^\circ; \theta = 45^\circ \Rightarrow e_u = \frac{2 \times 0.785}{40 \times 0.229} \times 40 \times (0 + 1 \times 1) = 6.85 \text{ cm}$$

Razmak uzengija će biti određen iz uslova zadovoljenja minimalnog procenta armiranja:

$$\mu_{uz} = \frac{m \times a_u^{(1)}}{b \times e_u} \Rightarrow e_u \leq \frac{2 \times 0.785}{40 \times 0.2 \times 10^{-2}} = 19.6 \text{ cm} \Rightarrow \text{usv. } e_u = 15 \text{ cm}$$

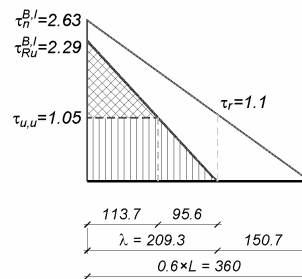
$$\tau_{u,u} = \frac{2 \times 0.785}{40 \times 15} \times 40 = 0.105 \frac{\text{kN}}{\text{cm}^2}$$

Dužina na kojoj su potrebni koso povijeni profili je dužina na kojoj je napon τ_{Ru} veći od napona koji prihvataju ovako usvojene uzengije:

$$\lambda_1 = \lambda \times \left(1 - \frac{\tau_{u,u}}{\tau_{Ru}}\right) = 209.3 \times \left(1 - \frac{0.105}{0.229}\right) = 113.7 \text{ cm}$$

$$H_{vu,k} = 40 \times \frac{0.229 - 0.105}{2} \times 113.7 = 283 \text{ kN}$$

$$A_{ak} = \frac{H_{vu,k}}{\sigma_v \times (\cos \alpha_k + \cot \theta \times \sin \alpha_k)} = \frac{283}{40 \times \sqrt{2}} = 5.00 \text{ cm}^2 \Rightarrow \text{usvojeno: } \mathbf{2R\check{O}22} \quad (7.60 \text{ cm}^2)$$



2.4 ANALIZA OPTEREĆENJA ZA POS 2

Greda je iste visine kao POS 3, a širina je usvojena tako da odgovara dimenziji opekar-skog proizvoda koji se koristi za fasadu (puna opeka širine 25 cm). Za datu spratnu visinu od $H_{sp} = 3.50$ m i datu fasadu (puna opeka + termoizolacija + kamen 3 cm na potkonstrukciji), težina fasade se dobija kao:

$$g_f = (H_{sp} - d) \times g_{25} + H_{sp} \times g_{kp} = (3.50 - 0.50) \times 4.60 + 3.50 \times 0.90 = 16.95 \text{ kN/m}$$

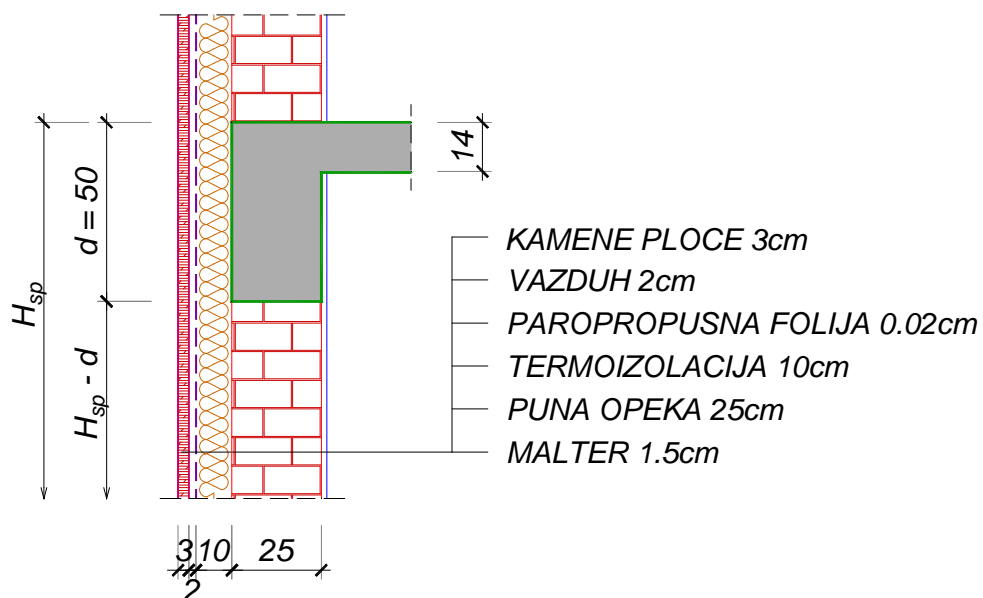
gde je: $g_{25} = 4.60 \text{ kN/m}^2$ – težina obostrano omalterisanog zida od pune opeke, a

$g_{kp} = 0.90 \text{ kN/m}^2$ – težina kamenih ploča debljine 3 cm na potkonstrukciji

Za datu fasadu i usvojene dimenzije grede $b/d = 25/50$ cm sledi:

- sopstvena težina POS 2	$0.25 \times 0.5 \times 25$	=	3.13 kN/m
- težina fasade	g_f	=	16.95 kN/m
- stalno opterećenje od POS 1	A_g	=	11.25 kN/m
ukupno, stalno opterećenje	g	=	31.33 kN/m
povremeno opterećenje od POS 1:	$A_p = p$	=	7.50 kN/m

Detalj fasade



2.5 PRELIMINARNO DIMENZIONISANJE POS 2

2.5.1 Dimenzionisanje prema momentu savijanja

$$q_u = 1.6 \times 31.33 + 1.8 \times 7.5 = 63.62 \text{ kN/m}$$

$$M_{u,1} = 63.62 \times 6.0^2 / 10 = 229.0 \text{ kNm - gornja zona, oslonac}$$

$$\text{pretp. } a_1 = 7 \text{ cm} \Rightarrow b/d/h = 25/50/43 \text{ cm}$$

$$k = \frac{43}{\sqrt{\frac{229.0 \times 10^2}{25 \times 2.05}}} = 2.034 \Rightarrow \begin{cases} \varepsilon_b / \varepsilon_a = 3.5 / 6.519\% \\ \mu = 28.278\% \end{cases}$$

$$A_a = 28.278 \times \frac{25 \times 43}{100} \times \frac{2.05}{40} = 15.58 \text{ cm}^2 \Rightarrow \text{usvojeno: } \mathbf{5R\text{\O}22} \text{ (19.01 cm}^2\text{)}$$

2.5.2 Kontrola glavnih napona zatezanja

$$T_u^{B,levo} = 0.6 \times 63.62 \times 6.0 = 229.0 \text{ kN} \Rightarrow \tau_n^{B,l} = \frac{229.0}{25 \times 0.9 \times 43} = 0.237 \frac{\text{kN}}{\text{cm}^2} \begin{cases} > \tau_r \\ < 3\tau_r \end{cases}$$

$$\lambda = 0.6 \times 600 \times \left(1 - \frac{0.11}{0.237}\right) = 192.7 \text{ cm}$$

$$\tau_{Ru}^{B,l} = \frac{3}{2} \times (0.237 - 0.11) = 0.190 \frac{\text{kN}}{\text{cm}^2}$$

$$\text{usvojeno: } m = 2; \alpha = 90^\circ; \theta = 45^\circ:$$

$$e_u = \frac{2 \times 0.503}{25 \times 0.190} \times 40 \times (0 + 1 \times 1) = 8.5 \text{ cm}$$

$$\text{usvojeno: } \mathbf{UR\text{\O}8/7.5}$$

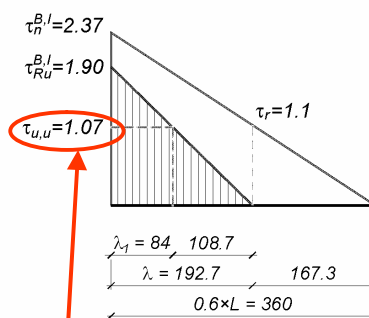
U bilo kojoj varijanti, s obzirom na relativno veliku dužinu osiguranja, uzengije će biti proređene na dvosečne UR\O8/15, koje mogu prihvatiti napon:

$$\mu = \frac{2 \times 0.503}{25 \times 15} = 0.268\% \Rightarrow \tau_{u,u} = \frac{2 \times 0.503}{25 \times 15} \times 40 = 0.107 \frac{\text{kN}}{\text{cm}^2}$$

Ovako usvojene uzengije nisu dovoljne na dužini:

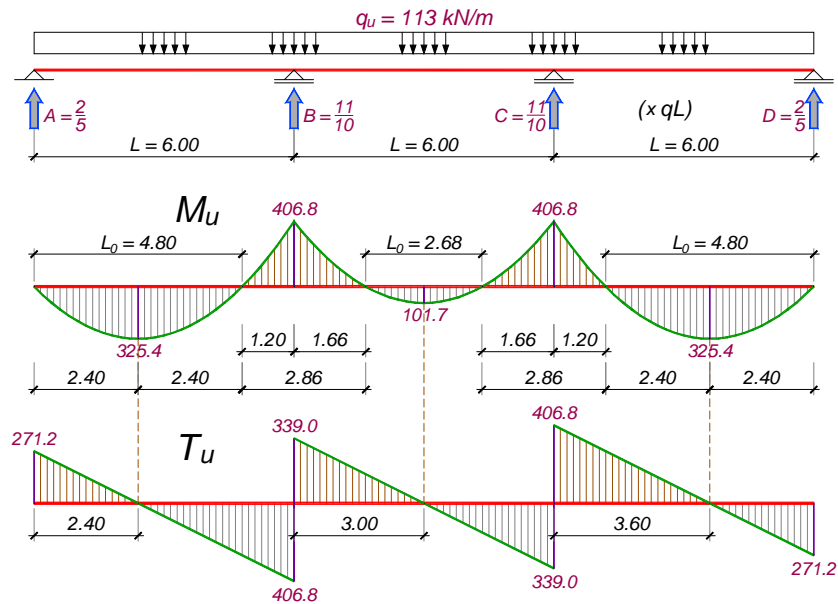
$$\lambda_1 = 192.7 \times \left(1 - \frac{0.107}{0.190}\right) = 84.0 \text{ cm}$$

Dakle, na dužini $\lambda_1 = 84 \text{ cm}$ konačno su usvojene udvojene uzengije 2UR\O8/15, a na preostalom delu dužine osiguranja jednostruke UR\O8/15.



POS 3 - granično opterećenje (1.6×G+1.8×P)

9



2.7.1.2 Preseci u krajnjim poljima

10

$$L_0 = 0.8 \times 600 = 480 \text{ cm} \Rightarrow B = \min. \left\{ \begin{array}{l} 40 + 20 \times 14 = 320 \\ 40 + 0.25 \times 480 = 160 \end{array} \right\} = 160 \text{ cm}$$

$$k = \frac{45}{\sqrt{\frac{325.4 \times 10^2}{160 \times 2.05}}} = 4.518 \Rightarrow \left\{ \begin{array}{l} \varepsilon_b / \varepsilon_a = 1.193 / 10\text{‰} \\ s = 0.107 \Rightarrow x = 0.107 \times 45 = 4.8 \text{ cm} < d_p = 14 \text{ cm} \\ \bar{\mu} = 5.092\% \end{array} \right.$$

$$A_a = 5.092 \times \frac{160 \times 45}{100} \times \frac{2.05}{40} = 18.79 \text{ cm}^2 \Rightarrow \text{usv.: } \mathbf{5R\text{Ø}22} \text{ (19.01 cm}^2\text{)}$$

2.7.1.3 Presek u srednjem polju

$$L_0 = \frac{L}{\sqrt{5}} = \frac{600}{\sqrt{5}} = 268 \text{ cm} \Rightarrow B = \min. \left\{ \begin{array}{l} 40 + 20 \times 14 = 320 \\ 40 + 0.25 \times 268 = 107 \end{array} \right\} = 107 \text{ cm}$$

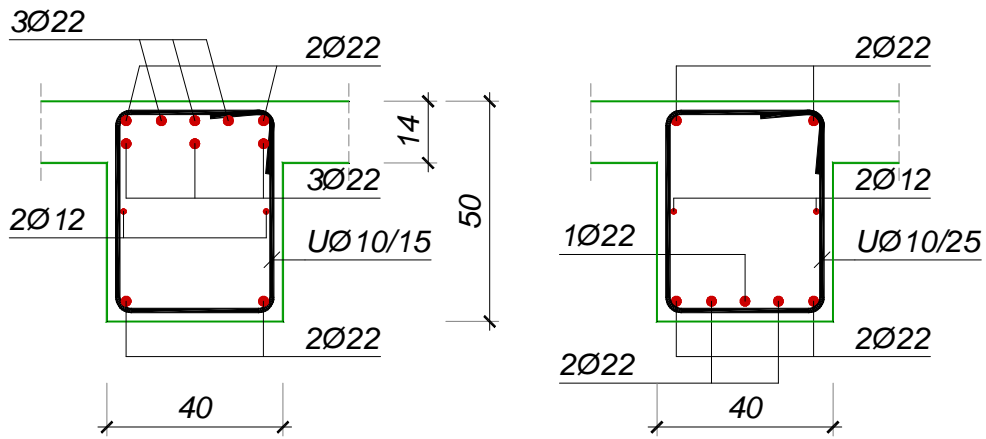
$$k = \frac{45}{\sqrt{\frac{101.7 \times 10^2}{107 \times 2.05}}} = 6.611 \Rightarrow \left\{ \begin{array}{l} \varepsilon_b / \varepsilon_a = 0.76 / 10\text{‰} \\ s = 0.071 \Rightarrow x = 0.071 \times 45 = 3.2 \text{ cm} < d_p = 14 \text{ cm} \\ \bar{\mu} = 2.345\% \end{array} \right.$$

$$A_a = 2.179 \times \frac{107 \times 45}{100} \times \frac{2.05}{40} = 5.79 \text{ cm}^2 > A_{a,\min} = 0.2 \times \frac{40 \times 50}{100} = 4.0 \text{ cm}^2$$

$$\text{usvojeno: } \mathbf{2R\text{Ø}22} \text{ (7.60 cm}^2\text{)}$$

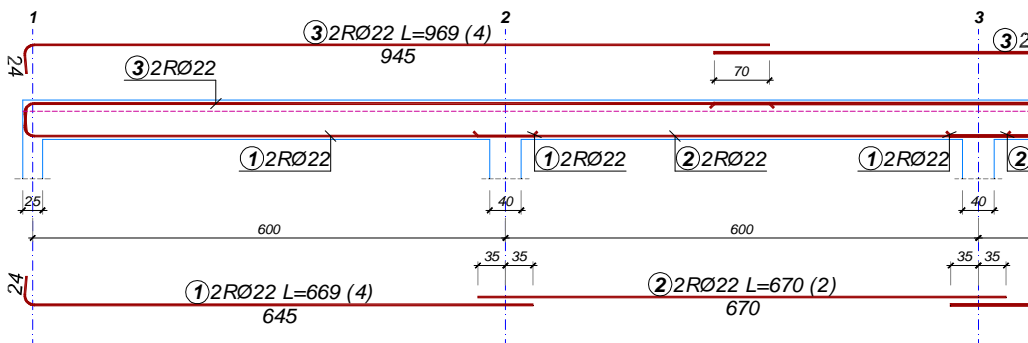
POS 3 – preseci nad osloncem i u krajnjem polju

11



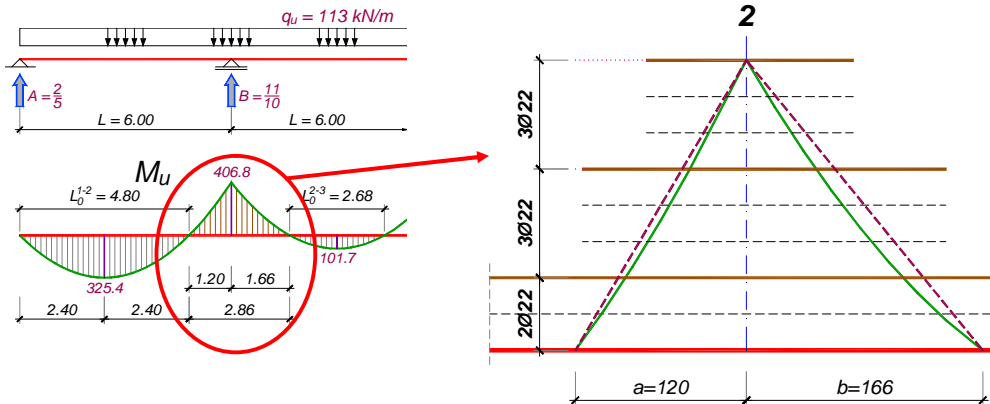
Armatura kontinualne grede – ugaone šipke

12



Procena dužine šipki u gornjoj zoni

13

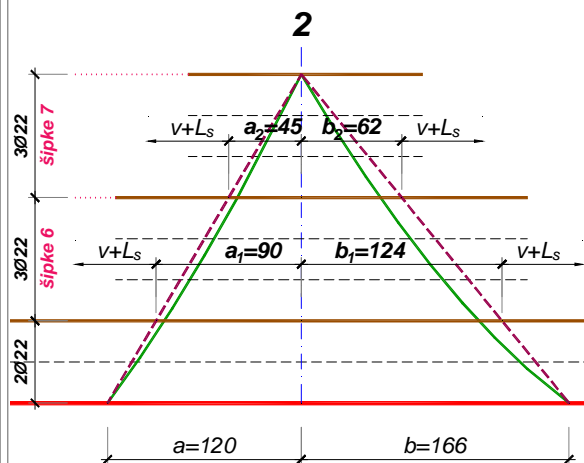


$$L_0^{1-2} = 0.8 \times L = 0.8 \times 600 = 480 \text{ cm} \Rightarrow a = L - L_0^{1-2} = 600 - 480 = 120 \text{ cm}$$

$$L_0^{2-3} = \frac{L}{\sqrt{5}} = \frac{600}{\sqrt{5}} = 268 \text{ cm} \Rightarrow b = \frac{L - L_0^{2-3}}{2} = \frac{600 - 268}{2} = 166 \text{ cm}$$

Procena dužine šipki u gornjoj zoni

14



$$v = 0.75 \times 43 \approx 32 \text{ cm}$$

$$MB 30 \Rightarrow \tau_p = 1.75 \text{ MPa}$$

$$L_{s1} = \frac{400}{4 \times 1.8 \times 1.75} \varnothing = 31.75 \times \varnothing$$

$$L_{s2} = 1.5 \times L_{s1} = 47.6 \times 2.2 \approx 105 \text{ cm}$$

$$v + L_{s2} = 32 + 105 = 137 \approx 140 \text{ cm}$$

$$a_1 = a \times \frac{6\varnothing 22}{8\varnothing 22} = 0.75 \times 120 = 90 \text{ cm}$$

$$a_2 = a \times \frac{3\varnothing 22}{8\varnothing 22} = 0.375 \times 120 = 45 \text{ cm}$$

$$b_1 = b \times \frac{6\varnothing 22}{8\varnothing 22} = 0.75 \times 166 = 124 \text{ cm}$$

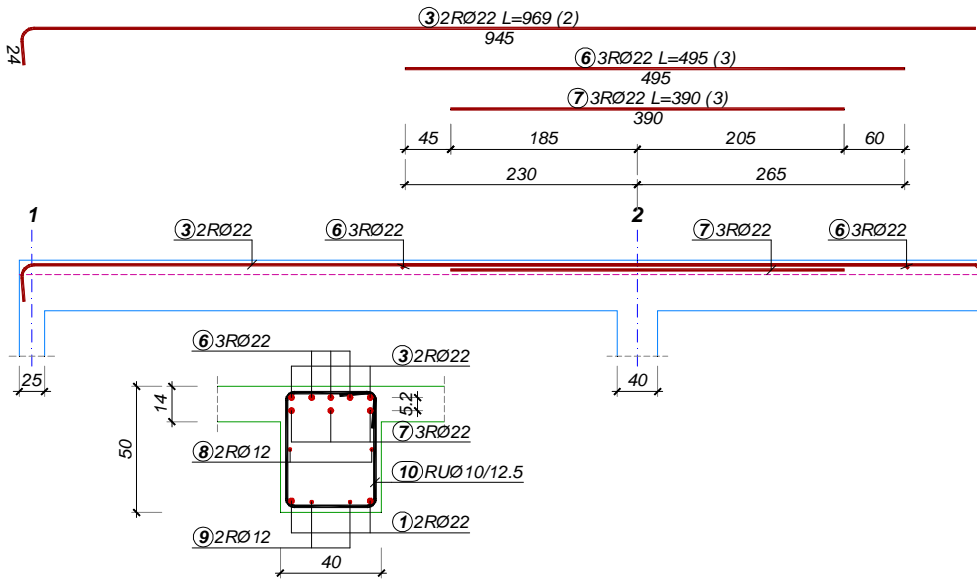
$$b_2 = b \times \frac{3\varnothing 22}{8\varnothing 22} = 0.375 \times 166 = 62 \text{ cm}$$

$$L^{\text{POS6}} = 140 + 90 + 124 + 140 = 494 \approx 495 \text{ cm}$$

$$L^{\text{POS7}} = 140 + 45 + 62 + 140 = 387 \approx 390 \text{ cm}$$

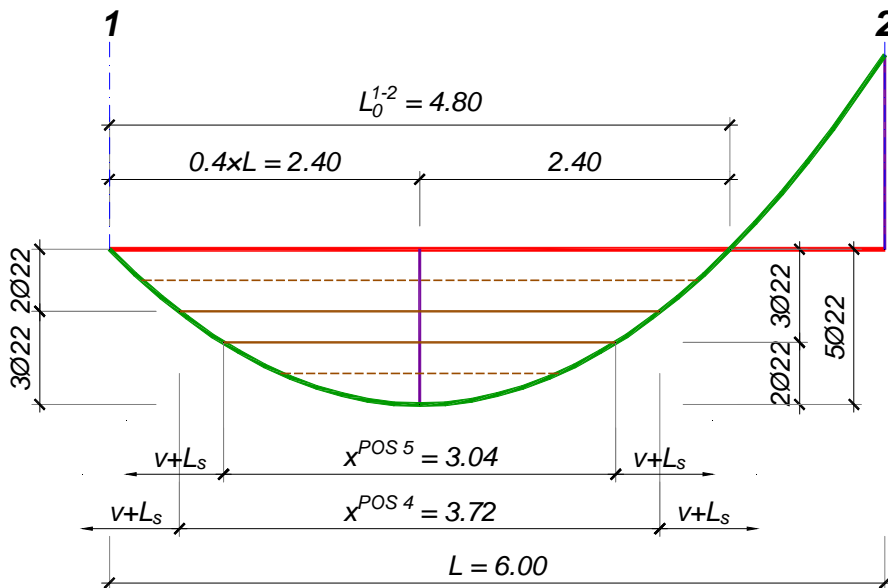
Procena dužine šipki u gornjoj zoni

15



Procena dužine šipki u donjoj zoni – krajnja polja

16



Procena dužine šipki u donjoj zoni

17

$$x^{POS5} = L_0 \times \sqrt{\frac{M_1}{M}} = L_0 \times \sqrt{\frac{2\emptyset22}{5\emptyset22}} = 4.80 \times \sqrt{0.4} = 3.04 \text{ m}$$

$$v + L_s = v + L_{s1} = 0.75 \times h + L_{s1} \approx 32 + 31.75 \times 2.2 \approx 102 \text{ cm}$$

$$L^{POS5} \approx v + L_s + x^{POS5} + v + L_s = 102 + 304 + 102 = 508 \approx 510 \text{ cm}$$

$$x^{POS4} = L_0 \times \sqrt{\frac{M_2}{M}} = L_0 \times \sqrt{\frac{3\emptyset22}{5\emptyset22}} = 4.80 \times \sqrt{0.6} = 3.72 \text{ m}$$

$$L^{POS4} \approx v + L_s + x_2 + v + L_s = 102 + 372 + 102 = 576 \approx 580 \text{ cm}$$

Šipke su simetrično postavljene u odnosu na mesto maksimalnog momenta u polju ($x = 2.4 \text{ m}$ od ose 1 ka osi 2)

Procena dužine šipki u donjoj zoni – krajnja polja

18

